

# USA Computing Olympiad



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## USACO 2024 JANUARY CONTEST, SILVER PROBLEM 1. COWMPETENCY

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 English (en) ▼

Farmer John is hiring a new herd leader for his cows. To that end, he has interviewed  $N$  ( $2 \leq N \leq 10^5$ ) cows for the position. After interviewing the  $i$ th candidate, he assigned the candidate an integer "cowmpetency" score  $c_i$  ranging from 1 to  $C$  inclusive ( $1 \leq C \leq 10^9$ ) that is correlated with their leadership abilities.

Because he has interviewed so many cows, Farmer John does not remember all of their cowmpetency scores. However, he does remember  $Q$  ( $1 \leq Q < N$ ) pairs of numbers  $(a_j, h_j)$  where cow  $h_j$  was the first cow with a **strictly greater** cowmpetency score than cows 1 through  $a_j$  (so  $1 \leq a_j < h_j \leq N$ ).

Farmer John now tells you the sequence  $c_1, \dots, c_N$  (where  $c_i = 0$  means that he has forgotten cow  $i$ 's cowmpetency score) and the  $Q$  pairs of  $(a_j, h_j)$ . Help him determine the **lexicographically smallest** sequence of cowmpetency scores consistent with this information, or that no such sequence exists! A sequence of scores is lexicographically smaller than another sequence of scores if it assigns a smaller score to the first cow at which the two sequences differ.

Each input contains  $T$  ( $1 \leq T \leq 20$ ) independent test cases. The sum of  $N$  across all test cases is guaranteed to not exceed  $3 \cdot 10^5$ .

### INPUT FORMAT (input arrives from the terminal / stdin):

The first line contains  $T$ , the number of independent test cases. Each test case is described as follows:

1. First, a line containing  $N$ ,  $Q$ , and  $C$ .
2. Next, a line containing the sequence  $c_1, \dots, c_N$  ( $0 \leq c_i \leq C$ ).
3. Finally,  $Q$  lines each containing a pair  $(a_j, h_j)$ . It is guaranteed that all  $a_j$  within a test case are distinct.

### OUTPUT FORMAT (print output to the terminal / stdout):

For each test case, output a single line containing the lexicographically smallest sequence of cowmpetency scores consistent with what Farmer John remembers, or  $-1$  if such a sequence does not exist.

### SAMPLE INPUT:

```
1
7 3 5
1 0 2 3 0 4 0
1 2
3 4
4 5
```

### SAMPLE OUTPUT:

```
1 2 2 3 4 4 1
```

We can see that the given output satisfies all of Farmer John's remembered pairs.

- $\max(c_1) = 1$ ,  $c_2 = 2$  and  $1 < 2$  so the first pair is satisfied
- $\max(c_1, c_2, c_3) = 2$ ,  $c_4 = 3$  and  $2 < 3$  so the second pair is satisfied
- $\max(c_1, c_2, c_3, c_4) = 3$ ,  $c_5 = 4$  and  $3 < 4$  so the third pair is satisfied

There are several other sequences consistent with Farmer John's memory, such as

```
1 2 2 3 5 4 1
1 2 2 3 4 4 5
```

However, none of these are lexicographically smaller than the given output.

### SAMPLE INPUT:

```
5
7 6 10
0 0 0 0 0 0 0
1 2
```

```

2 3
3 4
4 5
5 6
6 7
8 4 9
0 0 0 0 1 6 0 6
1 3
6 7
4 7
2 3
2 1 1
0 0
1 2
10 4 10
1 2 0 2 1 5 8 6 0 3
4 7
1 2
5 7
3 7
10 2 8
1 0 0 0 0 5 7 0 0 0
4 6
6 9

```

**SAMPLE OUTPUT:**

```

1 2 3 4 5 6 7
1 1 2 6 1 6 7 6
-1
1 2 5 2 1 5 8 6 1 3
-1

```

In test case 3, since  $C = 1$ , the only potential sequence is

```
1 1
```

However, in this case, cow 2 does not have a greater score than cow 1, so we cannot satisfy the condition.

In test case 5,  $a_1$  and  $h_1$  tell us that cow 6 is the first cow to have a strictly greater score than cows 1 through 4. Therefore, the largest score for cows 1 through 6 is that of cow 6: 5. Since cow 7 has a score of 7, cow 7 is the first cow to have a greater score than cows 1 through 6. So, the second statement that cow 9 is the first cow to have a greater score than cows 1 through 6 cannot be true.

**SCORING:**

- Input 3 satisfies  $N \leq 10$  and  $Q, C \leq 4$ .
- Inputs 4-8 satisfy  $N \leq 1000$ .
- Inputs 9-12 satisfy no additional constraints.

Problem credits: Suhas Nagar

Contest has ended. No further submissions allowed.